

# Reasoning about Object Capabilities with Logical Relations and Effect Parametricity

(EuroS&P 2016, Saarbrücken)

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December 2015



Object capabilities

Reasoning about Object Capabilities

Encapsulation, shared data, authority

Reasoning about Primitive I/O

Conclusion

Example: browser ad sandboxing:

$$\begin{aligned} rnode &\stackrel{\text{def}}{=} \text{func}(node, d)\{\dots\} \\ \text{initWebPage} &\stackrel{\text{def}}{=} \text{func}(document, ad) \\ &\left\{ \begin{array}{l} \text{let } (adNode = document.addChild("ad\_div")) \\ \text{let } (rAdNode = rnode(adNode, 0)) \\ ad.initialize(rAdNode) \end{array} \right\} \end{aligned}$$

- Fine-grained privilege separation.
- Control authority of arbitrary, untrusted, untyped code.
  - Just restrict what it has access to.
- Low tech, low overhead.
  - No types/...
  - Standard OO techniques/patterns.
- High-level OO languages or low-level assembly
- Applications:
  - sandboxing
  - fault isolation
  - auditability
  - etc.

A *capability-safe* language:

- Private state encapsulation.
- Primitive I/O through non-public objects (like *document*).
- No global mutable state.

Examples:

- E, Joe-E, Emily, Newspeak etc.
- JavaScript 5 (strict mode, after proper initialisation)?

$$\begin{aligned} rnode &\stackrel{\text{def}}{=} \text{func}(node, d)\{\dots\} \\ \text{initWebPage} &\stackrel{\text{def}}{=} \text{func}(\text{document}, ad) \\ &\left\{ \begin{array}{l} \text{let } (adNode = \text{document.addChild}(\text{"ad\_div"})) \\ \text{let } (rAdNode = rnode(adNode, 0)) \\ ad.\text{initialize}(rAdNode) \end{array} \right\} \end{aligned}$$

Are we 100% sure?

- What does the language guarantee precisely? Is it really capability-safe? What does that mean?
- What to ensure precisely?
- What can we rely on precisely?

OCap community:

- Reference graph
- “No Authority Amplification”
- “Only Connectivity Begets Connectivity”

Problem:

- Syntactic bound on authority.
- Ignores behavior.
- Necessary, but not sufficient!

What's the alternative?



What's the alternative?

...logical relations...  
...Kripke worlds...  
...modular reasoning...

But applications?



Programming Languages Researcher



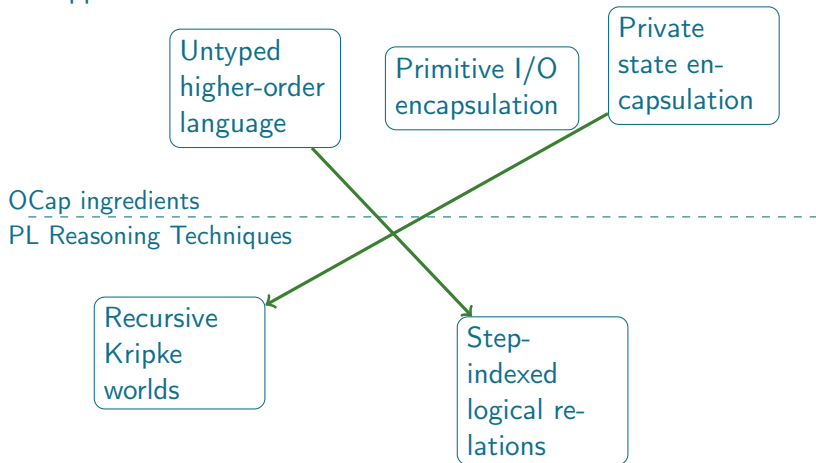
...privilege separation...  
...capability-safety...  
...security applications...

But how to reason?

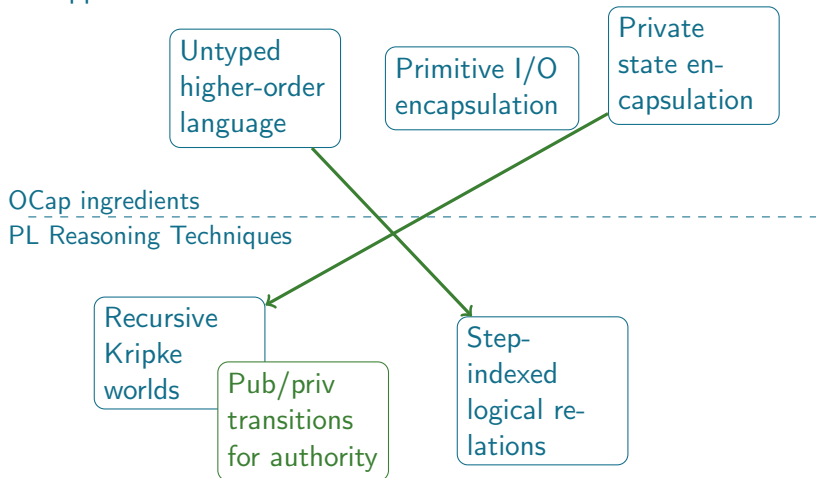


Security Researcher

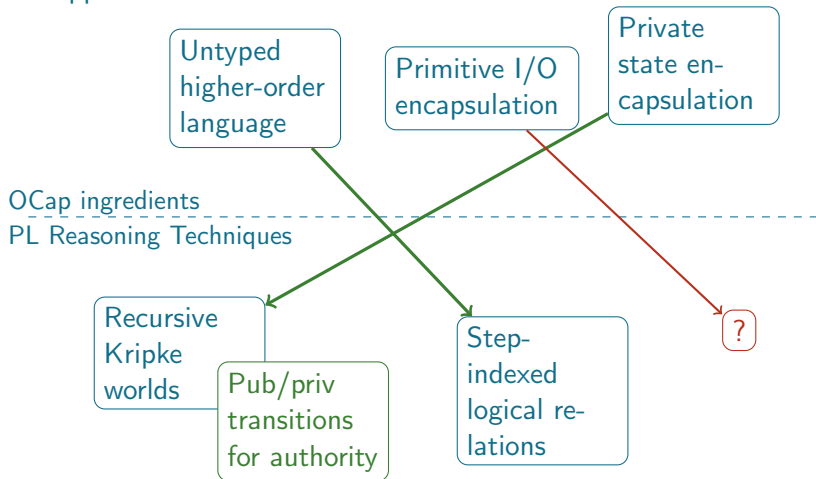
Our approach:



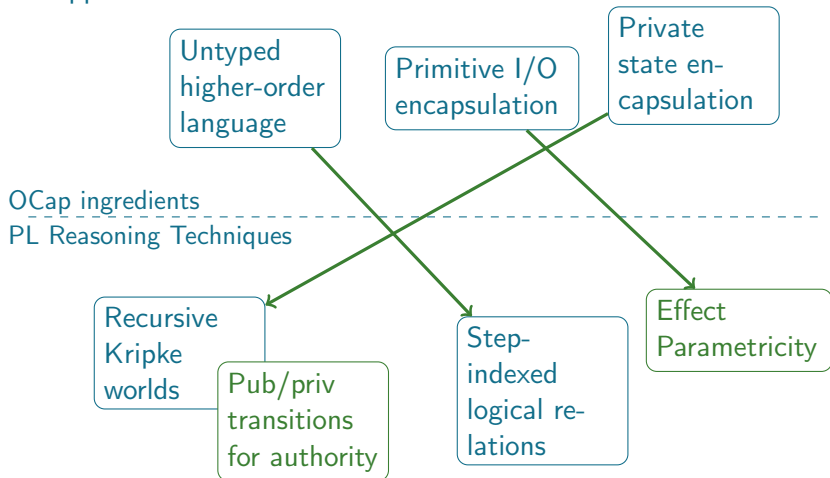
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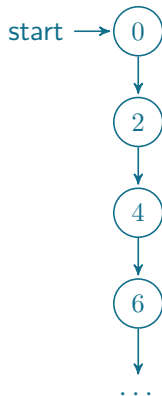


Our approach:



Register state machine to govern fresh data structure.

$ticketDispenser \stackrel{\text{def}}{=} \text{func}(attacker)$

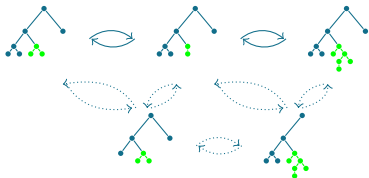
$$\left\{ \begin{array}{l} \text{let}(o = \text{ref } 0) \\ \quad \text{let} (dispTkt = \text{func}()\{ \\ \quad \quad \text{let} (v = \text{deref } o)\{o := v + 2; v\}\}) \\ \text{attacker}(dispTkt); \\ \text{deref } o \end{array} \right\}$$


Public transitions: accessible under current authority.

Private transitions: potentially accessible by others.

$$rnode \stackrel{\text{def}}{=} \text{func}(node, d)\{\dots\}$$

$$initWebPage \stackrel{\text{def}}{=} \text{func}(document, ad)$$

$$\left\{ \begin{array}{l} \text{let } (adNode = document.addChild("ad\_div")) \\ \text{let } (rAdNode = rnode(adNode, 0)) \\ ad.initialize(rAdNode) \end{array} \right\}$$


Effect interpretation: custom property about primitive effects

$$\rho \in \mathcal{P}(\text{Cap})$$

$$\mu \in \mathcal{P}(\text{Val}) \rightarrow \mathcal{P}(\text{Expr})$$

+ admissibility conditions...

Effect parametricity.

### Theorem (Fundamental Theorem for $\lambda_{JS}$ )

*If  $\Gamma, \Sigma \vdash e$  then for a valid effect interpretation  $(\mu, \rho)$  and for all  $n, \gamma$  and  $w$  with  $(n, w) \in \llbracket \Sigma \rrbracket_{\mu, \rho}$  and  $(n, \gamma) \in \llbracket \Gamma \rrbracket_{\mu, \rho}$   $w$ , we have that  $(n, \gamma(e))$  must be in  $\mathcal{E}[\mu \text{ JSVal}_{\mu, \rho}] w$ .*



- Capability Safety is:
  - Private state encapsulation.
  - Absence of global state.
  - Primitive I/O encapsulation.
- Modular reasoning in cap-safe language:
  - Reference graph dynamics is not enough
  - Logical relations to the rescue.
- Some novel features:
  - Authority over shared data using public/private transitions.
  - Effect parametricity.
- (Not shown: relational version)

- Build effect interpretations into Kripke worlds?
- A program logic?
- Apply to full JavaScript?

Worlds:

$$\text{IslandName} \stackrel{\text{def}}{=} \mathbb{N}$$

$$W \stackrel{\text{def}}{=} \{w \in \text{IslandName} \leftrightarrow \text{Island} \mid \text{dom}(w) \text{ finite}\}$$

$$\text{Island} \stackrel{\text{def}}{=} \left\{ \begin{array}{l} \iota = (s, \phi, \phi^{\text{pub}}, H) \mid s \in \text{State} \wedge \phi \subseteq \text{State}^2 \wedge \\ H \in \text{State} \rightarrow \text{StorePred} \wedge \phi^{\text{pub}} \subseteq \phi \wedge \\ \phi, \phi^{\text{pub}} \text{ reflexive and transitive} \end{array} \right\}$$

$$\text{StorePred} \stackrel{\text{def}}{=} \{\psi \in \hat{W} \rightarrow_{\text{mon,ne}} \text{UPred}(\text{Store})\}$$

$$\text{roll} : \frac{1}{2} \cdot W \cong \hat{W}$$

Effect interpretations:

$$\rho : W \rightarrow_{mon,ne} UPred(Loc)$$

$$\mu : (W \rightarrow_{mon,ne} UPred(Val)) \rightarrow_{ne} (W \rightarrow_{ne} Pred(Cmd)).$$

$JSVal_{\mu,\rho}$  predicate:

$$JSVal_{\mu,\rho} : W \rightarrow_{mon,ne} UPred(Val)$$

$$JSVal_{\mu,\rho} \stackrel{\text{def}}{=} Cnst \cup \rho \cup \{JSVal_{\mu,\rho}\} \cup ([JSVal_{\mu,\rho}] \rightarrow \mu JSVal_{\mu,\rho})$$

Admissibility conditions for effect interpretation:

- A-PURE: If  $(n, v) \in P w$  then  $(n, v) \in \mu P w$
- A-BIND: If  $(n, cmd) \in \mu P w$  and  $(n', E\langle v \rangle) \in \mathcal{E}[\mu P'] w'$  for all  $n' \leq n$ ,  $w' \sqsupseteq w$  and  $(n', v) \in P w'$ , then  $(n, E\langle cmd \rangle) \in \mathcal{E}[\mu P'] w$ .
- A-ASSIGN: If  $(n, v_1) \in \text{JSVal}_{\mu, \rho} w$  and  $(n, v_2) \in \text{JSVal}_{\mu, \rho} w$ , then  $(n, v_1 = v_2) \in \mu \text{JSVal}_{\mu, \rho} w$ .
- A-DEREF: If  $(n, v) \in \text{JSVal}_{\mu, \rho} w$ ,  $(n, \text{deref } v)$  must be in  $\mu \text{JSVal}_{\mu, \rho} w$ .
- A-REF: If  $(n, v) \in \text{JSVal}_{\mu, \rho} w$ , then  $(n, \text{ref } v) \in \mu \text{JSVal}_{\mu, \rho} w$ .