

# Softwaretechnik

## Lecture 18: Featherweight Java

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## Featherweight Java

The language shown in examples

Formal Definition

Operational Semantics

Typing Rules

# Type Safety of Java

- ▶ 1995 public presentation of Java
- ▶ Obtained importance very quickly
- ▶ Questions
  - ▶ Type safety?
  - ▶ Semantics of Java?
- ▶ 1997/98 resolved
  - ▶ Drossopoulou/Eisenbach
  - ▶ Flatt/Krishnamurthi/Felleisen
  - ▶ Igarashi/Pierce/Wadler (Featherweight Java, FJ)

# Featherweight Java

- ▶ Construction of a formal model:  
consideration of completeness and compactness
- ▶ FJ: minimal model (compactness)
- ▶ complete definition: one page
- ▶ ambition:
  - ▶ the most important language features
  - ▶ short proof of type soundness
  - ▶  $FJ \subseteq Java$

# The Language FJ

- ▶ class definition
- ▶ object creation **new**
- ▶ method call (*dynamic dispatch*), recursion with **this**
- ▶ field access
- ▶ type cast
- ▶ method *override*
- ▶ subtypes

# Omitted

- ▶ assignment
- ▶ interfaces
- ▶ *overloading*
- ▶ **super-calls**
- ▶ **null-references**
- ▶ primitive types
- ▶ abstract methods
- ▶ inner classes
- ▶ shadowing of fields of super classes
- ▶ access control (**private, public, protected**)
- ▶ *exceptions*
- ▶ concurrency
- ▶ reflection, generics, variable argument lists

# Example Programs

```
class A extends Object { A() { super (); } }
```

```
class B extends Object { B() { super (); } }
```

```
class Pair extends Object {
    Object fst;
    Object snd;
    // Constructor
    Pair (Object fst, Object snd) {
        super(); this.fst = fst; this.snd = snd;
    }
    // Method definition
    Pair setfst (Object newfst) {
        return new Pair (newfst, this.snd);
    }
}
```

# Explanation

- ▶ Class definition: always define super class
- ▶ Constructors:
  - ▶ one per class, always defined
  - ▶ arguments correspond to fields
  - ▶ always the same form:  
**super-call**, then copy the arguments into the fields
- ▶ field accesses and method calls **always** with receiver object
- ▶ method body: always in the form **return...**

# Examples for Evaluation

## Method call

```
new Pair (new A(), new B()).setfst (new B())
// will be evaluated to
new Pair (new B(), new B())
```

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```

## Type cast

```
((Pair) new Pair (new Pair (new A(), new B()),
                    new A()).fst).snd
```

- ▶ Type cast (Pair) is needed, because **new** Pair (...).fst has the type Object.

# Examples for Evaluation

## Field access

```
new Pair (new A (), new B ()).snd  
// will be evaluated to  
new B()
```

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## Field access

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```

## Method call

```
new Pair (new A(), new B()).setfst (new B())
```

yields a substitution

[**new** B()/**newfst**,    **new** Pair (**new** A(), **new** B())/**this**]

Evaluate the method body **new** Pair (**newfst**, **this.snd**) under this substitution.  
The substitution yields

```
new Pair (new B(), new Pair (new A(), new B()).snd)
```

# Examples of Evaluation

## Type cast

```
(Pair)new Pair (new A (), new B ())  
// evaluates to  
new Pair (new A (), new B ())
```

- ▶ Run-time check if Pair is a subtype of Pair.

# Examples of Evaluation

## Type cast

```
(Pair)new Pair (new A (), new B ())  
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new Pair (new A (), new B ())
```

- ▶ Run-time check if Pair is a subtype of Pair.

## Call-by-value evaluation

```
((Pair) new Pair (new Pair (new A(), new B ()), new A()).fst).snd  
// →  
((Pair) new Pair (new A(), new B ())).snd  
// →  
new Pair (new A(), new B ()).snd  
// →  
new B()
```

# Runtime Errors

## Access to non existing field

```
new A().fst
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No value, no evaluation rule matches

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new A().setfst (new B())
```

No value, no evaluation rule matches

## Failing type cast

```
(B)new A ()
```

- ▶ A is not subtype of B
- ⇒ no value, no evaluation rule matches

# Guarantees of Java's Type System

If a Java program is type correct, then

- ▶ all field accesses refer to existing fields
- ▶ all method calls refer to existing methods,
- ▶ **but** failing type casts are possible.

# Formal Definition

## Syntax

$CL ::=$		class definition
	<b>class</b> $C$ <b>extends</b> $D$ $\{C_1\ f_1; \dots\ K\ M_1\dots\}$	
$K ::=$		constructor definition
	$C(C_1\ f_1, \dots) \{super(g_1, \dots); this.f_1 = f_1; \dots\}$	
$M ::=$		method definition
	$C\ m(C_1\ x_1, \dots) \{return\ t;\}$	
$t ::=$		expressions
	$x$	variable
	$t.f$	field access
	$t.m(t_1, \dots)$	method call
	<b>new</b> $C(t_1, \dots)$	object creation
	$(C)\ t$	type cast
$v ::=$		values
	<b>new</b> $C(v_1, \dots)$	object creation

# Syntax—Conventions

- ▶ **this**
  - ▶ special variable, do not use it as field name or parameter
  - ▶ implicit bound in each method body
- ▶ sequences of field names, parameter names and method names include no repetition
- ▶ **class  $C$  extends  $D$  { $C_1 f_1; \dots K M_1 \dots$ }**
  - ▶ defines class  $C$  as subclass of  $D$
  - ▶ fields  $f_1 \dots$  with types  $C_1 \dots$
  - ▶ constructor  $K$
  - ▶ methods  $M_1 \dots$
  - ▶ fields from  $D$  will be added to  $C$ , shadowing is not supported

# Syntax—Conventions

- ▶  $C(D_1\ g_1, \dots, C_1\ f_1, \dots) \{ \mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots \}$ 
  - ▶ define the constructor of class  $C$
  - ▶ fully specified by the fields of  $C$  and the fields of the super classes.
  - ▶ number of parameters is equal to number of fields in  $C$  and all its super classes.
  - ▶ body start with  $\mathbf{super}(g_1, \dots)$ , where  $g_1, \dots$  corresponds to the fields of the super classes
- ▶  $D\ m(C_1\ x_1, \dots) \{ \mathbf{return}\ t; \}$ 
  - ▶ defines method  $m$
  - ▶ result type  $D$
  - ▶ parameter  $x_1 \dots$  with types  $C_1 \dots$
  - ▶ body is a **return** statement

# Class Table

- ▶ The *class table*  $CT$  is a map from class names to class definitions
  - ⇒ each class has exactly one definition
    - ▶ the  $CT$  is global, it corresponds to the program
    - ▶ “arbitrary but fixed”
- ▶ Each class except Object has a superclass
  - ▶ Object is not part of CT
  - ▶ Object has no fields
  - ▶ Object has no methods ( $\neq$  Java)
- ▶ The class table defines a subtype relation  $C <: D$  over class names
  - ▶ the reflexive and transitive closure of subclass definitions.

# Subtype Relation

$$\text{REFL } \frac{}{C \leqslant C}$$

$$\text{TRANS } \frac{C \leqslant D \quad D \leqslant E}{C \leqslant E}$$

$$\text{EXT } \frac{CT(C) = \mathbf{class}\ C\ \mathbf{extends}\ D\dots}{C \leqslant D}$$

# Consistency of CT

1.  $CT(C) = \mathbf{class}\ C\dots$  for all  $C \in \text{dom}(CT)$
2. Object  $\notin \text{dom}(CT)$
3. For each class name  $C$  mentioned in  $CT$ :  $C \in \text{dom}(CT) \cup \{\text{Object}\}$
4. The relation  $<$ : is antisymmetric (no cycles)

# Example: Classes Do Refer to Each Other

```
class Author extends Object {  
    String name; Book bk;  
  
    Author (String name, Book bk) {  
        super();  
        this.name = name;  
        this.bk = bk;  
    }  
}  
  
class Book extends Object {  
    String title; Author ath;  
  
    Book (String title, Author ath) {  
        super();  
        this.title = title;  
        this.ath = ath;  
    }  
}
```

# Auxiliary Definitions

Collect fields of classes

$$\text{fields}(\text{Object}) = \bullet$$

$$CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \}$$

$$\text{fields}(D) = D_1 g_1, \dots$$

---

$$\text{fields}(C) = D_1 g_1, \dots, C_1 f_1, \dots$$

- ▶  $\bullet$  — empty list
- ▶  $\text{fields}(\text{Author}) = \text{String name}; \text{Book bk};$
- ▶ Usage: evaluation steps, typing rules

# Auxiliary Definitions

Compute type of a method

$$\frac{CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ M_j = E \ m(E_1 \ x_1, \dots) \ \{\text{return } t; \}}{mtype(m, C) = (E_1, \dots) \rightarrow E}$$

$$\frac{CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ (\forall j) \ M_j \neq F \ m(F_1 \ x_1, \dots) \ \{\text{return } t; \}}{mtype(m, D) = (E_1, \dots) \rightarrow E}$$

$$\frac{}{mtype(m, C) = (E_1, \dots) \rightarrow E}$$

- ▶ Usage: typing rules

# Auxiliary Definitions

Determine body of a method

$$\frac{CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ M_j = E m(E_1 x_1, \dots) \{ \text{return } t; \}}{mbody(m, C) = (x_1 \dots, t)}$$

$$\frac{CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ (\forall j) M_j \neq F m(F_1 x_1, \dots) \{ \text{return } t; \} \\ mbody(m, D) = (y_1 \dots, u)}{mbody(m, C) = (y_1 \dots, u)}$$

- ▶ Usage: evaluation steps

# Auxiliary Definitions

Correct overriding of a method

$$\text{override}(m, \text{Object}, (E_1 \dots) \rightarrow E)$$

$$\frac{\begin{array}{c} CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ M_j = E m(E_1 x_1, \dots) \{ \text{return } t; \} \end{array}}{\text{override}(m, C, (E_1 \dots) \rightarrow E)}$$

$$\frac{\begin{array}{c} CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ (\forall j) M_j \neq F m(F_1 x_1, \dots) \{ \text{return } t; \} \end{array}}{\frac{\text{override}(m, D, (E_1, \dots) \rightarrow E)}{\text{override}(m, C, (E_1, \dots) \rightarrow E)}}$$

- ▶ Usage: typing rules

# Example

```
class Recording extends Object {
    int high; int today; int low;
    Recording (int high, int today, int low) { ... }
    int dHigh() { return this.high; }
    int dLow() { return this.low }
    String unit() { return "not set"; }
    String asString() {
        return String.valueOf(high)
            .concat("-")
            .concat (String.valueOf(low))
            .concat (unit());
    }
}
class Temperature extends ARecording {
    Temperature (int high, int today, int low) { super(high, today, low); }
    String unit() { return "°C"; }
}
```

- ▶  $\text{fields}(\text{Object}) = \bullet$
- ▶  $\text{fields}(\text{Temperature}) = \text{fields}(\text{Recording}) = \text{int high; int today; int low;}$
- ▶  $\text{mtype}(\text{unit}, \text{Recording}) = () \rightarrow \text{String}$
- ▶  $\text{mtype}(\text{unit}, \text{Temperature}) = () \rightarrow \text{String}$
- ▶  $\text{mtype}(\text{dHigh}, \text{Recording}) = () \rightarrow \text{int}$
- ▶  $\text{mtype}(\text{dHigh}, \text{Temperature}) = () \rightarrow \text{int}$
- ▶  $\text{override}(\text{dHigh}, \text{Object}, () \rightarrow \text{int})$
- ▶  $\text{override}(\text{dHigh}, \text{Recording}, () \rightarrow \text{int})$
- ▶  $\text{override}(\text{dHigh}, \text{Temperature}, () \rightarrow \text{int})$
- ▶  $\text{mbody}(\text{unit}, \text{Recording}) = (\varepsilon, \text{"not set"})$
- ▶  $\text{mtype}(\text{unit}, \text{Temperature}) = (\varepsilon, \text{"}^{\circ}\text{C"})$

# Operational Semantics (definition of the evaluation steps)

# Direct Evaluation Steps

- ▶ Evaluation: relation  $t \longrightarrow t'$  for one evaluation step

$$\text{E-PROJNEW} \frac{\text{fields}(C) = C_1\ f_1, \dots}{(\mathbf{new}\ C(v_1, \dots)).f_i \longrightarrow v_i}$$

$$\text{E-INVKNEW} \frac{mbody(m, C) = (x_1 \dots, t)}{(\mathbf{new}\ C(v_1, \dots)).m(u_1, \dots) \longrightarrow t[\mathbf{new}\ C(v_1, \dots)/\text{this}, u_1, \dots/x_1, \dots]}$$

$$\text{E-CASTNEW} \frac{C <: D}{(D)(\mathbf{new}\ C(v_1, \dots)) \longrightarrow \mathbf{new}\ C(v_1, \dots)}$$

# Evaluation Steps in Context

$$\text{E-FIELD} \frac{t \longrightarrow t'}{t.f \longrightarrow t'.f}$$

$$\text{E-INVK-RECV} \frac{t \longrightarrow t'}{t.m(t_1, \dots) \longrightarrow t'.m(t_1, \dots)}$$

$$\text{E-INVK-ARG} \frac{t_i \longrightarrow t'_i}{v.m(v_1, \dots, t_i, \dots) \longrightarrow v.m(v_1, \dots, t'_i, \dots)}$$

$$\text{E-NEW-ARG} \frac{t_i \longrightarrow t'_i}{\mathbf{new}\ C(v_1, \dots, t_i, \dots) \longrightarrow \mathbf{new}\ C(v_1, \dots, t'_i, \dots)}$$

$$\text{E-CAST} \frac{t \longrightarrow t'}{(C)t \longrightarrow (C)t'}$$

# Example: Evaluation Steps

```
((Pair) (new Pair (new Pair (new A(), new B()).setfst (new B()), new B()).fst)).fst
```

// → [E-Field], [E-Cast], [E-New-Arg], [E-InvkNew]

```
((Pair) (new Pair (new Pair (new B(), new B()), new B()).fst)).fst
```

// → [E-Field], [E-Cast], [E-ProjNew]

```
((Pair) (new Pair (new B(), new B()))).fst
```

// → [E-Field], [E-CastNew]

```
(new Pair (new B(), new B())).fst
```

// → [E-ProjNew]

```
new B()
```

# Typing Rules

# Typing Rules

## Overview of typing judgments

- ▶  $C <: D$   
 $C$  is subtype of  $D$
- ▶  $A \vdash t : C$   
Under type assumption  $A$ , the expression  $t$  has type  $C$ .
- ▶  $F m(C_1 x_1, \dots) \{ \text{return } t; \} \text{ OK in } C$   
Method declaration is accepted in class  $C$ .
- ▶ **class**  $C$  **extends**  $D \{ C_1 f_1; \dots K M_1 \dots \}$  **OK**  
Class declaration is accepted
- ▶ Type assumptions defined by

$$A ::= \emptyset \mid A, x : C$$

# Accepted Class Declaration

$$\frac{K = C(D_1\ g_1, \dots, C_1\ f_1, \dots) \ \{\mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots\} \\ \text{fields}(D) = D_1\ g_1 \dots \\ (\forall j) \ M_j \text{ OK in } C}{\text{class } C \text{ extends } D \ \{C_1\ f_1; \dots \ K\ M_1 \dots\}}$$

# Accepted Method Declaration

$$\frac{x_1 : C_1, \dots, \text{this} : C \vdash t : E \quad E \subset F \quad CT(C) = \text{class } C \text{ extends } D \dots \quad \overline{\text{override}(m, D, (C_1, \dots) \rightarrow F)}}{F m(C_1 \ x_1, \dots) \ \{\text{return } t; \} \text{ OK in } C}$$

# Expression Has Type

$$\text{T-VAR} \frac{x : C \in A}{A \vdash x : C}$$

$$\text{T-FIELD} \frac{A \vdash t : C \quad \text{fields}(C) = C_1 \ f_1, \dots}{A \vdash t.f_i : C_i}$$

$$\text{F-INVK} \frac{A \vdash t : C \quad (\forall i) \ A \vdash t_i : C_i \quad (\forall i) \ C_i \lessdot D_i \quad \text{mtype}(m, C) = (D_1, \dots) \rightarrow D}{A \vdash t.m(t_1, \dots) : D}$$

$$\text{F-NEW} \frac{(\forall i) \ A \vdash t_i : C_i \quad (\forall i) \ C_i \lessdot D_i \quad \text{fields}(C) = D_1 \ f_1, \dots}{A \vdash \mathbf{new} \ C(t_1, \dots) : C}$$

# Type Rules for Type Casts

$$\text{T-UCAST} \frac{A \vdash t : D \quad D \lessdot C}{A \vdash (C)t : C}$$

$$\text{T-DCAST} \frac{A \vdash t : D \quad C \lessdot D \quad C \neq D}{A \vdash (C)t : C}$$

# Type Safety for Featherweight Java

- ▶ “Preservation” and “Progress” yields type safety
- ▶ “Preservation”:  
If  $A \vdash t : C$  and  $t \rightarrow t'$ , then  $A \vdash t' : C'$  with  $C' \triangleleft C$ .
- ▶ “Progress”: (short version)  
If  $A \vdash t : C$ , then  $t \rightarrow t'$ , for some  $t'$ , or  $t \equiv v$  is a value, or  $t$  contains a subexpression  $e'$

$$e' \equiv (C)(\mathbf{new}~D(v_1, \dots))$$

with  $D \not\triangleleft C$ .

⇒

- ▶ All method calls and field accesses evaluate without errors.
- ▶ Type casts can fail.

# Problems in the Preservation Proof

Type casts destroy preservation

- ▶ Consider the expression  $(A) ((Object)\textbf{new } B())$
- ▶ It holds that  $\emptyset \vdash (A) ((Object)\textbf{new } B()): A$
- ▶ It holds that  $(A) ((Object)\textbf{new } B()) \longrightarrow (A) (\textbf{new } B())$
- ▶ But  $(A) (\textbf{new } B())$  has no type!

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- ▶ But  $(A) (\text{new } B())$  has no type!
- ▶ Workaround: add additional rule for this case (*stupid cast*)  
—subsequent evaluation step fails

$$\text{T-SCAST} \frac{A \vdash t : D \quad C \not\leq D \quad D \not\leq C}{A \vdash (C)t : C}$$

- ▶ We can prove preservation with this rule.

# Statement of Type Safety

If  $A \vdash t : C$ , then one of the following cases applies:

1.  $t$  does not terminate

i.e., there exists an infinite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow t_2 \longrightarrow \dots$$

2.  $t$  evaluates to a value  $v$  after a finite number of evaluation steps

i.e., there exists a finite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow \dots \longrightarrow t_n = v$$

3.  $t$  gets stuck at a failing cast

i.e., there exists a finite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow \dots \longrightarrow t_n$$

where  $t_n$  contains a subterm  $(C)(\mathbf{new}~D(v_1, \dots))$  such that  $D \not\leq C$ .