Functional Programming

https://proglang.informatik.uni-freiburg.de/teaching/functional-programming/2021/

Exercise Sheet 8 - GADTs

2021-07-21

Note: For the following exercises, you must turn on the GHC extension GADTs. To do this, add the following special comment (pragma) at the beginning of your Haskell source file:

```
{- # LANGUAGE GADTs # -}

In addition, it also recommended to use the pragma
{- # OPTIONS_GHC -fwarn-incomplete-patterns # -}
```

at the beginning of the file. This will make GHC warn you about pattern matchings that do not cover all the cases.

Exercise 1 (Safe List)

Define a list type SafeList that supports a "safe" head safeHead operation. That is, the type checker should allow the use of safeHead only if the argument is a non-empty SafeList:

```
safeHead (Cons 4 Nil) - ok
- safeHead Nil - Type error
```

This operation is called "safe" because it does not cause a runtime error on incorrect inputs, unlike head.

In addition, implement safeDrop and safeAppend in a meaningful way.

Exercise 2 (Stack Calculator)

We previously implemented a stack calculator. This one was quite simple:

- only arithmetic operations
- always returns 0 on underflow

Now, we can do it better! The stack should now have a finite size and contain both Int and Bool values. The stack programs should consist of the following commands:

1. Define the data type SProg so that it only accepts programs that can be executed without errors.

- 2. Implement a tag-free interpreter for SProg.
- 3. Write a SProg program that calculates the max of the two top elements. Write two more SProg toy programs and test them.
- 4. Now add the loop construct while to SProg.

```
sprog ::= ... | while sprog
-- Perform sprog as long as the top element of the stack is not True
```

- 5. Write a SProg program which, given two integers x, y at the top of the stack, places $x \mod y$ at the top of the stack. Use only the operations from the above syntax (and while, of course)
- 6. Give an example of a simple error-free stack program that you can *not* express with your SProg data type.