## Functional Programming

https://proglang.informatik.uni-freiburg.de/teaching/functional-programming/2022/

## Exercise Sheet 5

## Exercise 1 (Maybe, maybe not)

A very versatile data type available from the Prelude is Maybe. A value of type Maybe a holds either a value of type a or no value. The goal of this exercise is to make you comfortable working with Maybe values which you will come across in the following exercises.
The module Data.Maybe defines functions for working with Maybe values. Take a look through the documentation and choose three functions to implement yourself. You can check the solution yourself by clicking on the Source links.

## Exercise 2 (Unfolding)

As a dual to foldr there exists the function unfoldr : : (b -> Maybe (a, b)) -> b -> [a]
https://hackage.haskell.org/package/base-4.16.3.0/docs/Data-List.html\#v:unfoldr
Instead of reducing a list to a final result, unfoldr $f$ seed builds a new list: The elements of the list are created by repeatedly applying $f$ to the (updated) seed. Once $f$ seed returns Nothing the list is terminated.

1. Define unfoldr.
2. Using unfoldr, define map.
3. Using unfoldr, write a function range such that range $m \mathrm{n}$ produces the ordered list of integers from m to n (inclusively).

## Exercise 3 (Tries)

The goal of this exercise is to implement tries. Tries, or "prefix trees", are trees where each branch is indexed by a character. Each path in the trie then represent a list of characters, aka a string.

Note We will make use of the Map type from the containers library. A value of type Map k v is a dictionary/finite map from keys of type k to values of type v . The type and its functions are documented in Data.Map.Lazy. You will have to add the library to either your package.yaml file (stack) or the .cabal file (cabal), just as you did for QuickCheck.

We consider the following definition of tries, where each node contains a boolean (indicating if the string from the root node to this node is in the trie) and the branches of the tries represented as a map from characters to sub-tries.

## import qualified Data. Map as Map

data Trie $=$ Trie Bool (Map. Map Char Trie)

1. Implement the stubbed functions in Trie.hs linked on the lecture home page.

Additionally, derive or implement appropriate instances. You can also look through the API of Data.Set and Data.Map.Lazy for inspiration for additional functions.
2. Test your implementation using QuickCheck. Use the function fromList to generate arbitrary tries. You can consider tests such as "for any trie $t$ if I insert something in $t$ it is now a member."
Make sure, that your delete returns a minimal Trie: "if I insert a word winto some trie $t$ and I delete w again the result should be structurally equal to t."
3. The generalization from our Trie type, which stores words over Char, to storing words over any type a is relatively easy. As this translation is quite mechanical we will only consider what changes would be necessary.
a) Give the new data definition.
b) Are there required typeclass constraints? How do the type signatures change?
c) How do the function implementations change?
4. We now consider the case of a dictionary-trie, where each word is associated with a value. Create a new module containing the new data type TrieMap. Adapt the various functions and tests.

