

Softwaretechnik

Lecture 04: Featherweight Java

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Featherweight Java

The language shown in examples

Formal Definition

Operational Semantics

Typing Rules

Type Safety of Java

- ▶ 1995 public presentation of Java
- ▶ obtain importance very fast
- ▶ Questions
 - ▶ type safety?
 - ▶ What does Java mean?
- ▶ 1997/98 resolved
 - ▶ Drossopoulou/Eisenbach
 - ▶ Flatt/Krishnamurthi/Felleisen
 - ▶ Igarashi/Pierce/Wadler (Featherweight Java, FJ)

Featherweight Java

- ▶ Construction of a formal model:
consideration of completeness and compactness
- ▶ FJ: minimal model (compactness)
- ▶ complete definition: one page
- ▶ ambition:
 - ▶ the most important language features
 - ▶ short prove of type soundness
 - ▶ $FJ \subseteq Java$

The Language FJ

- ▶ class definition
- ▶ object creation **new**
- ▶ method call (*dynamic dispatch*), recursion with **this**
- ▶ field access
- ▶ type cast
- ▶ *override* of methods
- ▶ subtypes

Omitted

- ▶ assignments
- ▶ interfaces
- ▶ *overload*
- ▶ **super**-calls
- ▶ **null**-references
- ▶ primitive types
- ▶ abstract methods
- ▶ inner classes
- ▶ shadowing of fields of super classes
- ▶ access control (**private**, **public**, **protected**)
- ▶ *exceptions*
- ▶ concurrency
- ▶ reflections

Example Programs

```
class A extends Object { A() { super(); } }
```

```
class B extends Object { B() { super(); } }
```

```
class Pair extends Object {
    Object fst;
    Object snd;
    // Constructor
    Pair (Object fst, Object snd) {
        super(); this.fst = fst; this.snd = snd;
    }
    // Method definition
    Pair setfst (Object newfst) {
        return new Pair (newfst, this.snd);
    }
}
```

Explanation

- ▶ class definition: always define super class
- ▶ constructors:
 - ▶ one per class, always defined
 - ▶ arguments correspond to fields
 - ▶ always the same form: **super-call**, then copy the arguments into the fields
- ▶ field accesses and method calls **always** with recipient object
- ▶ method body: always in the form **return ...**

Examples for Evaluation

method call

```
new Pair (new A(), new B()).setfst (new B())
// will be evaluated to
new Pair (new B(), new B())
```

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```

type cast

```
((Pair) new Pair (new Pair (new A(), new B())),
new A()).fst).snd
```

- ▶ includes type cast (Pair)
- ▶ It's needed, because **new** Pair (...).fst has the type Object.

Examples for Evaluation

field access

```
new Pair (new A (), new B ()).snd  
// will be evaluated to  
new B()
```

Examples for Evaluation

field access

```
new Pair (new A (), new B ()).snd  
// will be evaluated to  
new B()
```

method call

```
new Pair (new A(), new B()).setfst (new B())
```

yields a substitution

[**new** B()/**newfst**, **new** Pair (**new** A(), **new** B())/**this**]

We have to evaluate the method body **new** Pair (**newfst**, **this.snd**) under this this substitution. The substitution yields

```
new Pair (new B(), new Pair (new A(), new B()).snd)
```

Examples of Evaluation

type cast

```
(Pair)new Pair (new A (), new B ())  
// wird ausgewertet nach  
new Pair (new A (), new B ())
```

- ▶ runtime check if Pair is a subtype of Pair.

Examples of Evaluation

type cast

```
(Pair)new Pair (new A (), new B ())  
// wird ausgewertet nach  
new Pair (new A (), new B ())
```

- ▶ runtime check if Pair is a subtype of Pair.

call-by-Value evaluation

```
((Pair) new Pair (new Pair (new A(), new B ()), new A()).fst).snd  
// →  
((Pair) new Pair (new A(), new B ())).snd  
// →  
new Pair (new A(), new B ()).snd  
// →  
new B()
```

Runtime Error

access to non existing field

```
new A().fst
```

no value, no evaluation rule matchs

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call of non existing method

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new A().setfst (new B())
```

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Runtime Error

access to non existing field

```
new A().fst
```

no value, no evaluation rule matchs

call of non existing method

```
new A().setfst (new B())
```

no value, no evaluation rule matchs

illegal type cast

```
(B)new A ()
```

- ▶ A is not subtype of B
- ⇒ no value, no evaluation rule matchs

Guarantees of Java's Type System

If a Java program is type correct, then

- ▶ access to non existing fields is not possible
- ▶ call of non existing methods is not possible, but
- ▶ illegal type casts are possible.

Formal Definition

Syntax

$CL ::=$	class definition
	class C extends $D \{ C_1\ f_1; \dots \ K\ M_1 \dots \}$
$K ::=$	constructor defintion
	$C(C_1\ f_1, \dots) \{\mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots\}$
$M ::=$	methode definition
	$C\ m(C_1\ x_1, \dots) \{\mathbf{return}\ t;\}$
$t ::=$	expressions
	x variable
	$t.f$ field access
	$t.m(t_1, \dots)$ method call
	new $C(t_1, \dots)$ object creation
	$(C)\ t$ type cast
$v ::=$	values
	new $C(v_1, \dots)$ object creation

Syntax—Conventions

- ▶ **this**
 - ▶ special variable, do not use it as field name or parameter
 - ▶ implicit bound in each method body
- ▶ sequences of field names, parameter names and method names include no repetition
- ▶ **class C extends D { $C_1 f_1; \dots K M_1 \dots$ }**
 - ▶ defines class C as subclass of D
 - ▶ fields $f_1 \dots$ with types $C_1 \dots$
 - ▶ constructor K
 - ▶ methods $M_1 \dots$
 - ▶ fields from D will be added to C , shadowing is not supported

Syntax—Conventions

- ▶ $C(D_1\ g_1, \dots, C_1\ f_1, \dots) \{ \mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots \}$
 - ▶ define the constructor of class C
 - ▶ It's fully specified from the fields from C and the fields from the super classes.
 - ▶ The count of parameters is equal to the count of fields in C and all its super classes.
 - ▶ body start with **super**(g_1, \dots), where g_1, \dots corresponds to the fields of the super classes
- ▶ $D\ m(C_1\ x_1, \dots) \{ \mathbf{return}\ t; \}$
 - ▶ defines method m
 - ▶ result type D
 - ▶ parameter $x_1 \dots$ with types $C_1 \dots$
 - ▶ body is a **return** statement

Class Table

- ▶ The *class table* CT is a map from class names to class definitions
 - ⇒ each class has exactly one definition
 - ▶ the CT is global, it corresponds to the program
 - ▶ “arbitrary but fixed”
- ▶ each class except Object has a super class
 - ▶ Object is not part of CT
 - ▶ Object has no fields
 - ▶ Object has no methods (\neq Java)
- ▶ The class table defines a subtype relation $C <: D$ over class names
 - ▶ the reflexive and transitive closure of subclass definitions.

Subtype Relation

$$\text{REFL } \frac{}{C \leqslant C}$$

$$\text{TRANS } \frac{C \leqslant D \quad D \leqslant E}{C \leqslant E}$$

$$\text{EXT } \frac{CT(C) = \mathbf{class}\ C\ \mathbf{extends}\ D\dots}{C \leqslant D}$$

Consistency of CT

1. $CT(C) = \mathbf{class}~C\dots$ for all $C \in \text{dom}(CT)$
2. Object $\notin \text{dom}(CT)$
3. For each class name C , that is mentioned in CT :
 $C \in \text{dom}(CT) \cup \{\text{Object}\}$
4. The relation $<$: is antisymmetric (no cycles)

Example: Classes Do Refer to Each Other

```
class Author extends Object {  
    String name; Book bk;  
  
    Author (String name, Book bk) {  
        super();  
        this.name = name;  
        this.bk = bk;  
    }  
}  
  
class Book extends Object {  
    String title; Author ath;  
  
    Book (String title, Author ath) {  
        super();  
        this.title = title;  
        this.ath = ath;  
    }  
}
```

Auxiliary Definitions

collect Fields of classes

$$\text{fields}(\text{Object}) = \bullet$$

$$CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \}$$

$$\text{fields}(D) = D_1 g_1, \dots$$

$$\text{fields}(C) = D_1 g_1, \dots, C_1 f_1, \dots$$

- ▶ \bullet — empty list
- ▶ $\text{fields}(\text{Author}) = \text{String name}; \text{Book bk};$
- ▶ Usage: evaluation steps, typing rules

Auxiliary Definitions

detect type of methods

$$\frac{CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ M_j = E \ m(E_1 \ x_1, \dots) \ \{\text{return } t; \}}{mtype(m, C) = (E_1, \dots) \rightarrow E}$$

$$\frac{CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ (\forall j) \ M_j \neq F \ m(F_1 \ x_1, \dots) \ \{\text{return } t; \}}{mtype(m, D) = (E_1, \dots) \rightarrow E}$$

$$\frac{}{mtype(m, C) = (E_1, \dots) \rightarrow E}$$

- ▶ Usage: typing rules

Auxiliary Definitions

determine body of method

$$\frac{CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ M_j = E m(E_1 x_1, \dots) \{ \text{return } t; \}}{mbody(m, C) = (x_1 \dots, t)}$$

$$\frac{CT(C) = \text{class } C \text{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \\ (\forall j) M_j \neq F m(F_1 x_1, \dots) \{ \text{return } t; \} \\ mbody(m, D) = (y_1 \dots, u)}{mbody(m, C) = (y_1 \dots, u)}$$

- ▶ Usage: evaluation steps

Auxiliary Definitions

correct overriding of methods

$$\text{override}(m, \text{Object}, (E_1 \dots) \rightarrow E)$$

$$\frac{\begin{array}{c} CT(C) = \mathbf{class}\ C\ \mathbf{extends}\ D\ \{C_1\ f_1; \dots\ K\ M_1\dots\} \\ M_j = E\ m(E_1\ x_1, \dots)\ \{\mathbf{return}\ t;\} \end{array}}{\text{override}(m, C, (E_1 \dots) \rightarrow E)}$$

$$\frac{\begin{array}{c} CT(C) = \mathbf{class}\ C\ \mathbf{extends}\ D\ \{C_1\ f_1; \dots\ K\ M_1\dots\} \\ (\forall j)\ M_j \neq F\ m(F_1\ x_1, \dots)\ \{\mathbf{return}\ t;\} \end{array}}{\frac{\text{override}(m, D, (E_1, \dots) \rightarrow E)}{\text{override}(m, C, (E_1, \dots) \rightarrow E)}}$$

- ▶ Usage: typing rules

Example

```
class Recording extends Object {
    int high; int today; int low;
    Recording (int high, int today, int low) { ... }
    int dHigh() { return this.high; }
    int dLow() { return this.low }
    String unit() { return "not set"; }
    String asString() {
        return String.valueOf(high)
            .concat("-")
            .concat (String.valueOf(low))
            .concat (unit());
    }
}
class Temperature extends ARecording {
    Temperature (int high, int today, int low) { super(high, today, low); }
    String unit() { return "°C"; }
}
```

- ▶ $\text{fields}(\text{Object}) = \bullet$
- ▶ $\text{fields}(\text{Temperature}) = \text{fields}(\text{Recording}) = \text{int high; int today; int low;}$
- ▶ $\text{mtype}(\text{unit}, \text{Recording}) = () \rightarrow \text{String}$
- ▶ $\text{mtype}(\text{unit}, \text{Temperature}) = () \rightarrow \text{String}$
- ▶ $\text{mtype}(\text{dHigh}, \text{Recording}) = () \rightarrow \text{int}$
- ▶ $\text{mtype}(\text{dHigh}, \text{Temperature}) = () \rightarrow \text{int}$
- ▶ $\text{override}(\text{dHigh}, \text{Object}, () \rightarrow \text{int})$
- ▶ $\text{override}(\text{dHigh}, \text{Recording}, () \rightarrow \text{int})$
- ▶ $\text{override}(\text{dHigh}, \text{Temperature}, () \rightarrow \text{int})$
- ▶ $\text{mbody}(\text{unit}, \text{Recording}) = (\varepsilon, \text{"not set"})$
- ▶ $\text{mtype}(\text{unit}, \text{Temperature}) = (\varepsilon, \text{"}^{\circ}\text{C"})$

Operational Semantics (definition of the evaluation steps)

Direct Evaluation Steps

- ▶ evaluation: relation $t \longrightarrow t'$ for one evaluation step

$$\text{E-PROJNEW} \frac{\text{fields}(C) = C_1\ f_1, \dots}{(\mathbf{new}\ C(v_1, \dots)).f_i \longrightarrow v_i}$$

$$\text{E-INVKNEW} \frac{mbody(m, C) = (x_1 \dots, t)}{(\mathbf{new}\ C(v_1, \dots)).m(u_1, \dots) \longrightarrow t[\mathbf{new}\ C(v_1, \dots)/\text{this}, u_1, \dots/x_1, \dots]}$$

$$\text{E-CASTNEW} \frac{C <: D}{(D)(\mathbf{new}\ C(v_1, \dots)) \longrightarrow \mathbf{new}\ C(v_1, \dots)}$$

Evaluation Steps in Context

$$\text{E-FIELD} \frac{t \longrightarrow t'}{t.f \longrightarrow t'.f}$$

$$\text{E-INVK-RECV} \frac{t \longrightarrow t'}{t.m(t_1, \dots) \longrightarrow t'.m(t_1, \dots)}$$

$$\text{E-INVK-ARG} \frac{t_i \longrightarrow t'_i}{v.m(v_1, \dots, t_i, \dots) \longrightarrow v.m(v_1, \dots, t'_i, \dots)}$$

$$\text{E-NEW-ARG} \frac{t_i \longrightarrow t'_i}{\mathbf{new}\ C(v_1, \dots, t_i, \dots) \longrightarrow \mathbf{new}\ C(v_1, \dots, t'_i, \dots)}$$

$$\text{E-CAST} \frac{t \longrightarrow t'}{(C)t \longrightarrow (C)t'}$$

Example: Evaluation Steps

((Pair) (**new** Pair (**new** Pair (**new** A(), **new** B()).setfst (**new** B()), **new** B()).fst)).fst

// → [E-Field], [E-Cast], [E-New-Arg], [E-InvkNew]

((Pair) (**new** Pair (**new** Pair (**new** B(), **new** B()), **new** B()).fst)).fst

// → [E-Field], [E-Cast], [E-ProjNew]

((Pair) (**new** Pair (**new** B(), **new** B()))).fst

// → [E-Field], [E-CastNew]

(**new** Pair (**new** B(), **new** B())).fst

// → [E-ProjNew]

new B()

Typing Rules

Typing Rules

involved type judgments

- ▶ $C <: D$
 C is subtype of D
- ▶ $A \vdash t : C$
The expression t has under type assumption A the type C .
- ▶ $F m(C_1 x_1, \dots) \{ \text{return } t; \}$ OK in C
Method declaration is accepted in class C .
- ▶ **class** C **extends** $D \{ C_1 f_1; \dots K M_1 \dots \}$ OK
Class declaration is accepted
- ▶ with

$$A ::= \emptyset \mid A, x : C$$

Accepted Class Declaration

$$\frac{K = C(D_1\ g_1, \dots, C_1\ f_1, \dots) \ \{\mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots\} \\ \text{fields}(D) = D_1\ g_1 \dots \\ (\forall j) \ M_j \text{ OK in } C}{\text{class } C \text{ extends } D \ \{C_1\ f_1; \dots \ K\ M_1 \dots\}}$$

Accepted Method Declaration

$$\frac{x_1 : C_1, \dots, \text{this} : C \vdash t : E \quad E \lessdot F \quad CT(C) = \text{class } C \text{ extends } D \dots \quad \overline{\text{override}(m, D, (C_1, \dots) \rightarrow F)}}{F m(C_1 \ x_1, \dots) \ \{\text{return } t; \} \text{ OK in } C}$$

Accepted Expressions Has a Type

$$\text{T-VAR} \frac{x : C \in A}{A \vdash x : C}$$

$$\text{T-FIELD} \frac{A \vdash t : C \quad \text{fields}(C) = C_1 \ f_1, \dots}{A \vdash t.f_i : C_i}$$

$$\text{F-INVK} \frac{A \vdash t : C \quad (\forall i) \ A \vdash t_i : C_i \quad (\forall i) \ C_i \lessdot D_i \quad \text{mtype}(m, C) = (D_1, \dots) \rightarrow D}{A \vdash t.m(t_1, \dots) : D}$$

$$\text{F-NEW} \frac{(\forall i) \ A \vdash t_i : C_i \quad (\forall i) \ C_i \lessdot D_i \quad \text{fields}(C) = D_1 \ f_1, \dots}{A \vdash \mathbf{new} \ C(t_1, \dots) : C}$$

Type Rules for Type Casts

$$\text{T-UCAST} \frac{A \vdash t : D \quad D \lessdot C}{A \vdash (C)t : C}$$

$$\text{T-DCAST} \frac{A \vdash t : D \quad C \lessdot D \quad C \neq D}{A \vdash (C)t : C}$$

Type Safety for Featherweight Java

- ▶ “Preservation” and “Progress” yields type safety
- ▶ “Preservation”:
If $A \vdash t : C$ and $t \longrightarrow t'$, then $A \vdash t' : C'$ with $C' \lessdot C$.
- ▶ “Progress”: (short version)
If $A \vdash t : C$, then $t \equiv v$ is a value or t contains a subexpression e'

$$e' \equiv (C)(\mathbf{new}~D(v_1, \dots))$$

with $D \not\propto C$.



- ▶ All method calls and field accesses evaluate without errors.
- ▶ Type casts can fail.

Problems in the Preservation Prove

Type casts destroy Preservation

- ▶ Lock at the expression $(A) ((Object)\text{new } B())$
- ▶ It holds $\emptyset \vdash (A) ((Object)\text{new } B()): A$
- ▶ It holds $(A) ((Object)\text{new } B()) \longrightarrow (A) (\text{new } B())$
- ▶ But $(A) (\text{new } B())$ has no type!

Problems in the Preservation Prove

Type casts destroy Preservation

- ▶ Lock at the expression $(A)((Object)\text{new } B())$
- ▶ It holds $\emptyset \vdash (A)((Object)\text{new } B()): A$
- ▶ It holds $(A)((Object)\text{new } B()) \longrightarrow (A)(\text{new } B())$
- ▶ But $(A)(\text{new } B())$ has no type!
- ▶ workaround: add additional rule for this case (*stupid cast*) —next evaluation step fail

$$\text{T-SCAST} \frac{A \vdash t : D \quad C \not\leq D \quad D \not\leq C}{A \vdash (C)t : C}$$

- ▶ We can prove preservation with this rule.

Statement of Type Safety

If $A \vdash t : C$, then one of the following cases applies:

1. t does not terminate

i.e. there exists an infinite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow t_2 \longrightarrow \dots$$

2. t returns a value v after finite evaluation steps

i.e. there exists a finite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow \dots \longrightarrow t_n = v$$

3. after finite evaluation steps t contains a sub term e , where

$$e \equiv (C)(\mathbf{new} \ D(v_1, \dots))$$

with $D \not\ll C$.