

## Softwaretechnik Lecture 21: Featherweight Java

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### Featherweight Java

The language shown in examples

Formal Definition

Operational Semantics

Typing Rules

## Type Safety of Java

- ▶ 1995 public presentation of Java
- ▶ obtain importance very fast
- ▶ Questions
  - ▶ type safety?
  - ▶ What does Java mean?
- ▶ 1997/98 resolved
  - ▶ Drossopoulou/Eisenbach
  - ▶ Flatt/Krishnamurthi/Felleisen
  - ▶ Igarashi/Pierce/Wadler (Featherweight Java, FJ)

## Featherweight Java

- ▶ Construction of a formal model:
  - consideration of completeness and compactness
- ▶ FJ: minimal model (compactness)
- ▶ complete definition: one page
- ▶ ambition:
  - ▶ the most important language features
  - ▶ short proof of type soundness
  - ▶  $FJ \subseteq Java$

## The Language FJ

- ▶ class definition
- ▶ object creation **new**
- ▶ method call (*dynamic dispatch*), recursion with **this**
- ▶ field access
- ▶ type cast
- ▶ *override* of methods
- ▶ subtypes

## Example Programs

```

class A extends Object { A() { super (); } }

class B extends Object { B() { super (); } }

class Pair extends Object {
  Object fst;
  Object snd;
  // Constructor
  Pair (Object fst, Object snd) {
    super(); this.fst = fst; this.snd = snd;
  }
  // Method definition
  Pair setfst (Object newfst) {
    return new Pair (newfst, this.snd);
  }
}

```

## Omitted

- ▶ assignments
- ▶ interfaces
- ▶ *overload*
- ▶ **super**-calls
- ▶ **null**-references
- ▶ primitive types
- ▶ abstract methods
- ▶ inner classes
- ▶ shadowing of fields of super classes
- ▶ access control (**private**, **public**, **protected**)
- ▶ *exceptions*
- ▶ concurrency
- ▶ reflections

## Explanation

- ▶ class definition: always define super class
- ▶ constructors:
  - ▶ one per class, always defined
  - ▶ arguments correspond to fields
  - ▶ always the same form: **super**-call, then copy the arguments into the fields
- ▶ field accesses and method calls **always** with recipient object
- ▶ method body: always in the form **return**...

## Examples for Evaluation

### method call

```
new Pair (new A(), new B()).setfst (new B())
// will be evaluated to
new Pair (new B(), new B())
```

## Examples for Evaluation

### field access

```
new Pair (new A (), new B ()).snd
// will be evaluated to
new B()
```

## Examples for Evaluation

### method call

```
new Pair (new A(), new B()).setfst (new B())
// will be evaluated to
new Pair (new B(), new B())
```

### type cast

```
((Pair) new Pair (new Pair (new A(), new B ()),
new A()).fst).snd
```

- ▶ includes type cast (Pair)
- ▶ It's needed, because `new Pair (...).fst` has the type `Object`.

## Examples for Evaluation

### field access

```
new Pair (new A (), new B ()).snd
// will be evaluated to
new B()
```

### method call

```
new Pair (new A(), new B()).setfst (new B())
```

yields a substitution

$$[\text{new B()}/\text{newfst}, \text{new Pair (new A(), new B())}/\text{this}]$$

We have to evaluate the method body `new Pair (newfst, this.snd)` under this substitution. The substitution yields

```
new Pair (new B(), new Pair (new A(), new B()).snd)
```

## Examples of Evaluation

### type cast

```
(Pair)new Pair (new A (), new B ())
// evaluates to
new Pair (new A (), new B ())
```

- ▶ runtime check if Pair is a subtype of Pair.

## Runtime Error

### access to non existing field

```
new A().fst
```

no value, no evaluation rule matches

## Examples of Evaluation

### type cast

```
(Pair)new Pair (new A (), new B ())
// evaluates to
new Pair (new A (), new B ())
```

- ▶ runtime check if Pair is a subtype of Pair.

### call-by-Value evaluation

```
((Pair) new Pair (new Pair (new A(), new B ()), new A()).fst).snd
// →
((Pair) new Pair (new A(), new B ())).snd
// →
new Pair (new A(), new B ()).snd
// →
new B()
```

## Runtime Error

### access to non existing field

```
new A().fst
```

no value, no evaluation rule matches

### call of non existing method

```
new A().setfst (new B())
```

no value, no evaluation rule matches

## Runtime Error

access to non existing field

```
new A().fst
```

no value, no evaluation rule matches

call of non existing method

```
new A().setfst (new B())
```

no value, no evaluation rule matches

failing type cast

```
(B)new A ()
```

▶ A is not subtype of B

⇒ no value, no evaluation rule matches

## Formal Definition

## Guarantees of Java's Type System

If a Java program is type correct, then

- ▶ all field accesses refer to existing fields
- ▶ all method calls refer to existing methods, but
- ▶ failing type casts are possible.

## Syntax

$CL$	::=	class definition
		<b>class</b> $C$ <b>extends</b> $D$ $\{C_1 f_1; \dots K M_1 \dots\}$
$K$	::=	constructor definition
		$C(C_1 f_1, \dots) \{\mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots\}$
$M$	::=	method definition
		$C m(C_1 x_1, \dots) \{\mathbf{return} t; \}$
$t$	::=	expressions
		$x$ variable
		$t.f$ field access
		$t.m(t_1, \dots)$ method call
		<b>new</b> $C(t_1, \dots)$ object creation
		$(C) t$ type cast
$v$	::=	values
		<b>new</b> $C(v_1, \dots)$ object creation

## Syntax—Conventions

- ▶ **this**
  - ▶ special variable, do not use it as field name or parameter
  - ▶ implicit bound in each method body
- ▶ sequences of field names, parameter names and method names include no repetition
- ▶ **class**  $C$  **extends**  $D$   $\{C_1 f_1; \dots K M_1 \dots\}$ 
  - ▶ defines class  $C$  as subclass of  $D$
  - ▶ fields  $f_1 \dots$  with types  $C_1 \dots$
  - ▶ constructor  $K$
  - ▶ methods  $M_1 \dots$
  - ▶ fields from  $D$  will be added to  $C$ , shadowing is not supported

## Syntax—Conventions

- ▶  $C(D_1 g_1, \dots, C_1 f_1, \dots) \{\mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots\}$ 
  - ▶ define the constructor of class  $C$
  - ▶ fully specified by the fields of  $C$  and the fields of the super classes.
  - ▶ number of parameters is equal to number of fields in  $C$  and all its super classes.
  - ▶ body start with **super**( $g_1, \dots$ ), where  $g_1, \dots$  corresponds to the fields of the super classes
- ▶  $D m(C_1 x_1, \dots) \{\mathbf{return} t; \}$ 
  - ▶ defines method  $m$
  - ▶ result type  $D$
  - ▶ parameter  $x_1 \dots$  with types  $C_1 \dots$
  - ▶ body is a **return** statement

## Class Table

- ▶ The *class table*  $CT$  is a map from class names to class definitions
  - $\Rightarrow$  each class has exactly one definition
    - ▶ the  $CT$  is global, it corresponds to the program
    - ▶ “arbitrary but fixed”
- ▶ Each class except Object has a superclass
  - ▶ Object is not part of  $CT$
  - ▶ Object has no fields
  - ▶ Object has no methods ( $\neq$  Java)
- ▶ The class table defines a subtype relation  $C \prec: D$  over class names
  - ▶ the reflexive and transitive closure of subclass definitions.

## Subtype Relation

$$\text{REFL} \frac{}{C \prec: C}$$

$$\text{TRANS} \frac{C \prec: D \quad D \prec: E}{C \prec: E}$$

$$\text{EXT} \frac{CT(C) = \mathbf{class} \ C \ \mathbf{extends} \ D \ \dots}{C \prec: D}$$

## Consistency of CT

1.  $CT(C) = \mathbf{class} C \dots$  for all  $C \in dom(CT)$
2.  $\mathbf{Object} \notin dom(CT)$
3. For each class name  $C$  mentioned in  $CT$ :  $C \in dom(CT) \cup \{\mathbf{Object}\}$
4. The relation  $\leq$ : is antisymmetric (no cycles)

## Auxiliary Definitions

collect Fields of classes

$$fields(\mathbf{Object}) = \bullet$$

$$\frac{CT(C) = \mathbf{class} C \text{ extends } D \{C_1 f_1; \dots K M_1 \dots\} \quad fields(D) = D_1 g_1, \dots}{fields(C) = D_1 g_1, \dots, C_1 f_1, \dots}$$

- ▶  $\bullet$  — empty list
- ▶  $fields(\mathbf{Author}) = \text{String name}; \text{Book bk};$
- ▶ Usage: evaluation steps, typing rules

## Example: Classes Do Refer to Each Other

```

class Author extends Object {
  String name; Book bk;

  Author (String name, Book bk) {
    super();
    this.name = name;
    this.bk = bk;
  }
}

class Book extends Object {
  String title; Author ath;

  Book (String title, Author ath) {
    super();
    this.title = title;
    this.ath = ath;
  }
}

```

## Auxiliary Definitions

detect type of methods

$$\frac{CT(C) = \mathbf{class} C \text{ extends } D \{C_1 f_1; \dots K M_1 \dots\} \quad M_j = E m(E_1 x_1, \dots) \{\mathbf{return} t;\}}{mtype(m, C) = (E_1, \dots) \rightarrow E}$$

$$\frac{CT(C) = \mathbf{class} C \text{ extends } D \{C_1 f_1; \dots K M_1 \dots\} \quad (\forall j) M_j \neq F m(F_1 x_1, \dots) \{\mathbf{return} t;\}}{mtype(m, D) = (E_1, \dots) \rightarrow E}$$

- ▶ Usage: typing rules

## Auxiliary Definitions

determine body of method

$$\frac{CT(C) = \mathbf{class } C \mathbf{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \quad M_j = E m(E_1 x_1, \dots) \{ \mathbf{return } t; \}}{mbody(m, C) = (x_1 \dots, t)}$$

$$\frac{CT(C) = \mathbf{class } C \mathbf{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \quad (\forall j) M_j \neq F m(F_1 x_1, \dots) \{ \mathbf{return } t; \} \quad mbody(m, D) = (y_1 \dots, u)}{mbody(m, C) = (y_1 \dots, u)}$$

- Usage: evaluation steps

## Example

```

class Recording extends Object {
  int high; int today; int low;
  Recording (int high, int today, int low) { ... }
  int dHigh() { return this.high; }
  int dLow() { return this.low }
  String unit() { return "not set"; }
  String asString() {
    return String.valueOf(high)
      .concat("—")
      .concat (String.valueOf(low))
      .concat (unit());
  }
}
class Temperature extends ARecording {
  Temperature (int high, int today, int low) { super(high, today, low); }
  String unit() { return "°C"; }
}

```

## Auxiliary Definitions

correct overriding of methods

$override(m, \mathbf{Object}, (E_1 \dots) \rightarrow E)$

$$\frac{CT(C) = \mathbf{class } C \mathbf{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \quad M_j = E m(E_1 x_1, \dots) \{ \mathbf{return } t; \}}{override(m, C, (E_1 \dots) \rightarrow E)}$$

$$\frac{CT(C) = \mathbf{class } C \mathbf{ extends } D \{ C_1 f_1; \dots K M_1 \dots \} \quad (\forall j) M_j \neq F m(F_1 x_1, \dots) \{ \mathbf{return } t; \} \quad override(m, D, (E_1, \dots) \rightarrow E)}{override(m, C, (E_1, \dots) \rightarrow E)}$$

- Usage: typing rules

- $fields(\mathbf{Object}) = \bullet$
- $fields(\mathbf{Temperature}) = fields(\mathbf{Recording}) = \text{int high; int today; int low;}$
- $mtype(\text{unit}, \mathbf{Recording}) = () \rightarrow \mathbf{String}$
- $mtype(\text{unit}, \mathbf{Temperature}) = () \rightarrow \mathbf{String}$
- $mtype(\text{dHigh}, \mathbf{Recording}) = () \rightarrow \mathbf{int}$
- $mtype(\text{dHigh}, \mathbf{Temperature}) = () \rightarrow \mathbf{int}$
- $override(\text{dHigh}, \mathbf{Object}, () \rightarrow \mathbf{int})$
- $override(\text{dHigh}, \mathbf{Recording}, () \rightarrow \mathbf{int})$
- $override(\text{dHigh}, \mathbf{Temperature}, () \rightarrow \mathbf{int})$
- $mbody(\text{unit}, \mathbf{Recording}) = (\varepsilon, \text{"not set"})$
- $mtype(\text{unit}, \mathbf{Temperature}) = (\varepsilon, \text{"°C"})$



# Operational Semantics (definition of the evaluation steps)

- evaluation: relation  $t \longrightarrow t'$  for one evaluation step

$$\text{E-PROJNEW} \frac{\text{fields}(C) = C_1 f_1, \dots}{(\text{new } C(v_1, \dots)).f_i \longrightarrow v_i}$$

$$\text{E-INVKNEW} \frac{\text{mbody}(m, C) = (x_1 \dots, t)}{(\text{new } C(v_1, \dots)).m(u_1, \dots) \longrightarrow t[\text{new } C(v_1, \dots)/\text{this}, u_1, \dots/x_1, \dots]}$$

$$\text{E-CASTNEW} \frac{C <: D}{(D)(\text{new } C(v_1, \dots)) \longrightarrow \text{new } C(v_1, \dots)}$$

## Evaluation Steps in Context

$$\text{E-FIELD} \frac{t \longrightarrow t'}{t.f \longrightarrow t'.f}$$

$$\text{E-INVK-RECV} \frac{t \longrightarrow t'}{t.m(t_1, \dots) \longrightarrow t'.m(t_1, \dots)}$$

$$\text{E-INVK-ARG} \frac{t_i \longrightarrow t'_i}{v.m(v_1, \dots, t_i, \dots) \longrightarrow v.m(v_1, \dots, t'_i, \dots)}$$

$$\text{E-NEW-ARG} \frac{t_i \longrightarrow t'_i}{\text{new } C(v_1, \dots, t_i, \dots) \longrightarrow \text{new } C(v_1, \dots, t'_i, \dots)}$$

$$\text{E-CAST} \frac{t \longrightarrow t'}{(C)t \longrightarrow (C)t'}$$

## Direct Evaluation Steps

## Example: Evaluation Steps

```

((Pair) (new Pair (new Pair (new A(), new B()).setfst (new B()), new B()).fst)).fst
// → [E-Field], [E-Cast], [E-New-Arg], [E-InvkNew]

((Pair) (new Pair (new Pair (new B(), new B()), new B()).fst)).fst
// → [E-Field], [E-Cast], [E-ProjNew]

((Pair) (new Pair (new B(), new B()))).fst
// → [E-Field], [E-CastNew]

(new Pair (new B(), new B())).fst
// → [E-ProjNew]

new B()

```

# Typing Rules

## Typing Rules

involved type judgments

- ▶  $C <: D$   
 $C$  is subtype of  $D$
- ▶  $A \vdash t : C$   
 Under type assumption  $A$ , the expression  $t$  has type  $C$ .
- ▶  $F m(C_1 x_1, \dots) \{\mathbf{return} t; \}$  OK in  $C$   
 Method declaration is accepted in class  $C$ .
- ▶ **class**  $C$  **extends**  $D \{C_1 f_1; \dots K M_1 \dots \}$  OK  
 Class declaration is accepted
- ▶ Type assumptions defined by

$$A ::= \emptyset \mid A, x : C$$

## Accepted Class Declaration

$$\frac{K = C(D_1 g_1, \dots, C_1 f_1, \dots) \{\mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots\} \quad \begin{array}{l} \mathit{fields}(D) = D_1 g_1 \dots \\ (\forall j) M_j \text{ OK in } C \end{array}}{\mathbf{class} \ C \ \mathbf{extends} \ D \ \{C_1 f_1; \dots K M_1 \dots \}}$$

## Accepted Method Declaration

$$\frac{x_1 : C_1, \dots, \mathbf{this} : C \vdash t : E \quad E <: F \quad CT(C) = \mathbf{class} \ C \ \mathbf{extends} \ D \dots \quad \mathit{override}(m, D, (C_1, \dots) \rightarrow F)}{F m(C_1 x_1, \dots) \{\mathbf{return} \ t; \} \text{ OK in } C}$$

## Expression Has Type

$$\text{T-VAR} \frac{x : C \in A}{A \vdash x : C}$$

$$\text{T-FIELD} \frac{A \vdash t : C \quad \text{fields}(C) = C_1 f_1, \dots}{A \vdash t.f_i : C_i}$$

$$\text{F-INVK} \frac{A \vdash t : C \quad (\forall i) A \vdash t_i : C_i \quad (\forall i) C_i \leq D_i \quad \text{mtype}(m, C) = (D_1, \dots) \rightarrow D}{A \vdash t.m(t_1, \dots) : D}$$

$$\text{F-NEW} \frac{(\forall i) A \vdash t_i : C_i \quad (\forall i) C_i \leq D_i \quad \text{fields}(C) = D_1 f_1, \dots}{A \vdash \mathbf{new} C(t_1, \dots) : C}$$

## Type Rules for Type Casts

$$\text{T-UCAST} \frac{A \vdash t : D \quad D \leq C}{A \vdash (C)t : C}$$

$$\text{T-DCAST} \frac{A \vdash t : D \quad C \leq D \quad C \neq D}{A \vdash (C)t : C}$$

## Type Safety for Featherweight Java

- ▶ “Preservation” and “Progress” yields type safety
- ▶ “Preservation”:  
If  $A \vdash t : C$  and  $t \longrightarrow t'$ , then  $A \vdash t' : C'$  with  $C' \leq C$ .
- ▶ “Progress”: (short version)  
If  $A \vdash t : C$ , then  $t \equiv v$  is a value or  $t$  contains a subexpression  $e'$

$$e' \equiv (C)(\mathbf{new} D(v_1, \dots))$$

with  $D \not\leq C$ .

⇒

- ▶ All method calls and field accesses evaluate without errors.
- ▶ Type casts can fail.

## Problems in the Preservation Proof

Type casts destroy preservation

- ▶ Consider the expression  $(A) ((\text{Object})\mathbf{new} B())$
- ▶ It holds  $\emptyset \vdash (A) ((\text{Object})\mathbf{new} B()) : A$
- ▶ It holds  $(A) ((\text{Object})\mathbf{new} B()) \longrightarrow (A) (\mathbf{new} B())$
- ▶ But  $(A) (\mathbf{new} B())$  has no type!

## Problems in the Preservation Proof

Type casts destroy preservation

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- ▶ It holds  $(A) ((\text{Object})\text{new } B()) \longrightarrow (A) (\text{new } B())$
- ▶ But  $(A) (\text{new } B())$  has no type!
- ▶ workaround: add additional rule for this case (*stupid cast*) —next evaluation step fail

$$\text{T-SC}_{\text{AST}} \frac{A \vdash t : D \quad C \not\vdash D \quad D \not\vdash C}{A \vdash (C)t : C}$$

- ▶ We can prove preservation with this rule.

## Statement of Type Safety

If  $A \vdash t : C$ , then one of the following cases applies:

1.  $t$  does not terminate  
i.e., there exists an infinite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow t_2 \longrightarrow \dots$$

2.  $t$  evaluates to a value  $v$  after a finite number of evaluation steps  
i.e., there exists a finite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow \dots \longrightarrow t_n = v$$

3.  $t$  gets stuck at a failing cast  
i.e., there exists a finite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow \dots \longrightarrow t_n$$

where  $t_n$  contains a subterm  $(C)(\text{new } D(v_1, \dots))$  such that  $D \not\vdash C$ .