

# Software Engineering

## Lecture 18: Featherweight Java

Peter Thiemann

University of Freiburg, Germany

15.07.2013

# Contents

## Featherweight Java

The language shown in examples

Formal Definition

Operational Semantics

Typing Rules

# Type Safety of Java

- ▶ 1995 public presentation of Java
- ▶ Obtained importance very quickly
- ▶ Questions
  - ▶ Type safety?
  - ▶ Semantics of Java?
- ▶ 1997/98 resolved
  - ▶ Drossopoulou/Eisenbach
  - ▶ Flatt/Krishnamurthi/Felleisen
  - ▶ Igarashi/Pierce/Wadler (Featherweight Java, FJ)

# Featherweight Java

- ▶ Construction of a formal model:  
consideration of completeness and compactness
- ▶ FJ: minimal model (compactness)
- ▶ complete definition: one page
- ▶ ambition:
  - ▶ the most important language features
  - ▶ short proof of type soundness
  - ▶  $FJ \subseteq Java$

# The Language FJ

- ▶ class definition
- ▶ object creation **new**
- ▶ method call (*dynamic dispatch*), recursion with **this**
- ▶ field access
- ▶ type cast
- ▶ method *override*
- ▶ subtypes

# Omitted

- ▶ assignment
- ▶ interfaces
- ▶ *overloading*
- ▶ **super**-calls
- ▶ **null**-references
- ▶ primitive types
- ▶ abstract methods
- ▶ inner classes
- ▶ shadowing of fields of super classes
- ▶ access control (**private**, **public**, **protected**)
- ▶ *exceptions*
- ▶ concurrency
- ▶ reflection, generics, variable argument lists

## Example Programs

```
class A extends Object { A() { super (); } }
```

```
class B extends Object { B() { super (); } }
```

```
class Pair extends Object {  
  Object fst;  
  Object snd;  
  // Constructor  
  Pair (Object fst, Object snd) {  
    super(); this.fst = fst; this.snd = snd;  
  }  
  // Method definition  
  Pair setfst (Object newfst) {  
    return new Pair (newfst, this.snd);  
  }  
}
```

# Explanation

- ▶ Class definition: always define super class
- ▶ Constructors:
  - ▶ one per class, always defined
  - ▶ arguments correspond to fields
  - ▶ always the same form:  
**super**-call, then copy the arguments into the fields
- ▶ field accesses and method calls **always** with receiver object
- ▶ method body: always in the form **return**...



# Examples for Evaluation

## Method call

```
new Pair (new A(), new B()).setfst (new B())  
// will be evaluated to  
new Pair (new B(), new B())
```

# Examples for Evaluation

## Method call

```
new Pair (new A(), new B()).setfst (new B())
// will be evaluated to
new Pair (new B(), new B())
```

## Type cast

```
((Pair) new Pair (new Pair (new A(), new B ()),
                 new A()).fst).snd
```

- ▶ Type cast (Pair) is needed, because `new Pair (...).fst` has the type Object.

# Examples for Evaluation

## Field access

```
new Pair (new A (), new B ()).snd  
// will be evaluated to  
new B()
```

# Examples for Evaluation

## Field access

```
new Pair (new A (), new B ()).snd
// will be evaluated to
new B()
```

## Method call

```
new Pair (new A(), new B()).setfst (new B())
```

yields a substitution

$[\mathbf{new\ B()} / \mathbf{newfst}, \quad \mathbf{new\ Pair\ (\mathbf{new\ A}(), \mathbf{new\ B}())} / \mathbf{this}]$

Evaluate the method body `new Pair (newfst, this.snd)` under this substitution.  
The substitution yields

```
new Pair (new B(), new Pair (new A(), new B()).snd)
```

# Examples of Evaluation

## Type cast

```
(Pair)new Pair (new A (), new B ())  
// evaluates to  
new Pair (new A (), new B ())
```

- ▶ Run-time check if Pair is a subtype of Pair.

## Examples of Evaluation

### Type cast

```
(Pair) new Pair (new A (), new B ())
// evaluates to
new Pair (new A (), new B ())
```

- ▶ Run-time check if Pair is a subtype of Pair.

### Call-by-value evaluation

```
((Pair) new Pair (new Pair (new A(), new B ()), new A()).fst).snd
// →
((Pair) new Pair (new A(), new B ())).snd
// →
new Pair (new A(), new B ()).snd
// →
new B()
```

# Runtime Errors

## Access to non existing field

```
new A().fst
```

No value, no evaluation rule matches

# Runtime Errors

## Access to non existing field

```
new A().fst
```

No value, no evaluation rule matches

## Call of non-existing method

```
new A().setfst (new B())
```

No value, no evaluation rule matches



# Runtime Errors

## Access to non existing field

```
new A().fst
```

No value, no evaluation rule matches

## Call of non-existing method

```
new A().setfst (new B())
```

No value, no evaluation rule matches

## Failing type cast

```
(B)new A ()
```

- ▶ A is not subtype of B
- ⇒ no value, no evaluation rule matches

# Guarantees of Java's Type System

If a Java program is type correct, then

- ▶ all field accesses refer to existing fields
- ▶ all method calls refer to existing methods,
- ▶ **but** failing type casts are possible.

# Formal Definition

## Syntax

$CL$	$::=$	class definition
		<b>class</b> $C$ <b>extends</b> $D$ $\{ C_1 f_1; \dots K M_1 \dots \}$
$K$	$::=$	constructor definition
		$C(C_1 f_1, \dots) \{ \mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots \}$
$M$	$::=$	method definition
		$C m(C_1 x_1, \dots) \{ \mathbf{return} t; \}$
$t$	$::=$	expressions
		$x$ variable
		$t.f$ field access
		$t.m(t_1, \dots)$ method call
		<b>new</b> $C(t_1, \dots)$ object creation
		$(C) t$ type cast
$v$	$::=$	values
		<b>new</b> $C(v_1, \dots)$ object creation

# Syntax—Conventions

- ▶ **this**
  - ▶ special variable, do not use it as field name or parameter
  - ▶ implicit bound in each method body
- ▶ sequences of field names, parameter names and method names include no repetition
- ▶ **class  $C$  extends  $D$   $\{C_1 f_1; \dots K M_1 \dots\}$** 
  - ▶ defines class  $C$  as subclass of  $D$
  - ▶ fields  $f_1 \dots$  with types  $C_1 \dots$
  - ▶ constructor  $K$
  - ▶ methods  $M_1 \dots$
  - ▶ fields from  $D$  will be added to  $C$ , shadowing is not supported

# Syntax—Conventions

- ▶  $C(D_1\ g_1, \dots, C_1\ f_1, \dots)$  {**super**( $g_1, \dots$ ); **this**. $f_1 = f_1; \dots$ }
  - ▶ define the constructor of class  $C$
  - ▶ fully specified by the fields of  $C$  and the fields of the super classes.
  - ▶ number of parameters is equal to number of fields in  $C$  and all its super classes.
  - ▶ body start with **super**( $g_1, \dots$ ), where  $g_1, \dots$  corresponds to the fields of the super classes
- ▶  $D\ m(C_1\ x_1, \dots)$  {**return**  $t$ ; }
  - ▶ defines method  $m$
  - ▶ result type  $D$
  - ▶ parameter  $x_1 \dots$  with types  $C_1 \dots$
  - ▶ body is a **return** statement

# Class Table

- ▶ The *class table*  $CT$  is a map from class names to class definitions
  - ⇒ each class has exactly one definition
    - ▶ the  $CT$  is global, it corresponds to the program
    - ▶ “arbitrary but fixed”
- ▶ Each class except `Object` has a superclass
  - ▶ `Object` is not part of  $CT$
  - ▶ `Object` has no fields
  - ▶ `Object` has no methods ( $\neq$  Java)
- ▶ The class table defines a subtype relation  $C \prec: D$  over class names
  - ▶ the reflexive and transitive closure of subclass definitions.

# Subtype Relation

$$\text{REFL} \\ C <: C$$

$$\text{TRANS} \\ \frac{C <: D \quad D <: E}{C <: E}$$

$$\text{EXT} \\ \frac{CT(C) = \mathbf{class\ } C \mathbf{ extends\ } D \dots}{C <: D}$$



# Subtype Relation

$$\text{REFL} \\ C <: C$$

$$\text{TRANS} \\ \frac{C <: D \quad D <: E}{C <: E}$$

$$\text{EXT} \\ \frac{CT(C) = \mathbf{class\ } C \mathbf{ extends\ } D \dots}{C <: D}$$

## Java: Assignment compatibility

If  $C <: D$ , then

- ▶ a  $C$ -value can be assigned to a  $D$ -variable and
- ▶ a  $C$ -value can be passed as a  $D$ -parameter.

# Intermezzo: Extension for Interfaces

Not part of FJ

$$\frac{\text{IMPL} \quad CT(C) = \mathbf{class} \ C \ \mathbf{implements} \ I \dots}{C <: I}$$

$$\frac{\text{IEXT} \quad CT(I) = \mathbf{interface} \ I \ \mathbf{extends} \ J \dots}{I <: J}$$

# Consistency of CT

1.  $CT(C) = \mathbf{class} C \dots$  for all  $C \in dom(CT)$
2.  $\mathbf{Object} \notin dom(CT)$
3. For each class name  $C$  mentioned in  $CT$ :  $C \in dom(CT) \cup \{\mathbf{Object}\}$
4. The relation  $<$ : is antisymmetric (no cycles)

## Example: Classes Do Refer to Each Other

```
class Author extends Object {  
  String name; Book bk;  
  
  Author (String name, Book bk) {  
    super();  
    this.name = name;  
    this.bk = bk;  
  }  
}  
  
class Book extends Object {  
  String title; Author ath;  
  
  Book (String title, Author ath) {  
    super();  
    this.title = title;  
    this.ath = ath;  
  }  
}
```

# Auxiliary Definitions

Collect fields of classes

$$fields(\text{Object}) = \bullet$$

$$\frac{CT(C) = \mathbf{class\ } C \mathbf{\ extends\ } D \{ C_1\ f_1; \dots\ K\ M_1 \dots \} \quad fields(D) = D_1\ g_1, \dots}{fields(C) = D_1\ g_1, \dots, C_1\ f_1, \dots}$$

- ▶  $\bullet$  — empty list
- ▶  $fields(\text{Author}) = \text{String name; Book bk;}$
- ▶ Usage: evaluation steps, typing rules

# Auxiliary Definitions

Compute type of a method

$$\frac{CT(C) = \mathbf{class} \ C \ \mathbf{extends} \ D \ \{C_1 \ f_1; \dots \ K \ M_1 \dots \} \\ M_j = E \ m(E_1 \ x_1, \dots) \ \{\mathbf{return} \ t; \}}{mtype(m, C) = (E_1, \dots) \rightarrow E}$$

$$\frac{CT(C) = \mathbf{class} \ C \ \mathbf{extends} \ D \ \{C_1 \ f_1; \dots \ K \ M_1 \dots \} \\ (\forall j) \ M_j \neq F \ m(F_1 \ x_1, \dots) \ \{\mathbf{return} \ t; \} \quad mtype(m, D) = (E_1, \dots) \rightarrow E}{mtype(m, C) = (E_1, \dots) \rightarrow E}$$

- Usage: typing rules

# Auxiliary Definitions

Determine body of a method

$$\frac{CT(C) = \mathbf{class\ } C \mathbf{ extends\ } D \{ C_1\ f_1; \dots\ K\ M_1 \dots \} \\ M_j = E\ m(E_1\ x_1, \dots) \{ \mathbf{return\ } t; \}}{mbody(m, C) = (x_1 \dots, t)}$$

$$\frac{CT(C) = \mathbf{class\ } C \mathbf{ extends\ } D \{ C_1\ f_1; \dots\ K\ M_1 \dots \} \\ (\forall j)\ M_j \neq F\ m(F_1\ x_1, \dots) \{ \mathbf{return\ } t; \} \quad mbody(m, D) = (y_1 \dots, u)}{mbody(m, C) = (y_1 \dots, u)}$$

- Usage: evaluation steps

# Auxiliary Definitions

Correct overriding of a method

$$\text{override}(m, \text{Object}, (E_1 \dots) \rightarrow E)$$

$$\frac{CT(C) = \mathbf{class} \ C \ \mathbf{extends} \ D \ \{ C_1 \ f_1; \dots \ K \ M_1 \dots \} \\ M_j = E \ m(E_1 \ x_1, \dots) \ \{\mathbf{return} \ t; \}}{\text{override}(m, C, (E_1 \dots) \rightarrow E)}$$

$$\frac{CT(C) = \mathbf{class} \ C \ \mathbf{extends} \ D \ \{ C_1 \ f_1; \dots \ K \ M_1 \dots \} \\ (\forall j) \ M_j \neq F \ m(F_1 \ x_1, \dots) \ \{\mathbf{return} \ t; \} \quad \text{override}(m, D, (E_1, \dots) \rightarrow E)}{\text{override}(m, C, (E_1, \dots) \rightarrow E)}$$

- ▶ Usage: typing rules



# Example

```

class Recording extends Object {
  int high; int today; int low;
  Recording (int high, int today, int low) { ... }
  int dHigh() { return this.high; }
  int dLow() { return this.low }
  String unit() { return "not set"; }
  String asString() {
    return String.valueOf(high)
      .concat("–")
      .concat (String.valueOf(low))
      .concat (unit());
  }
}

class Temperature extends ARecording {
  Temperature (int high, int today, int low) { super(high, today, low); }
  String unit() { return "°C"; }
}

```

- ▶  $fields(Object) = \bullet$
- ▶  $fields(Temperature) = fields(Recording) = \text{int high}; \text{int today}; \text{int low};$
- ▶  $mtype(\text{unit}, Recording) = () \rightarrow \text{String}$
- ▶  $mtype(\text{unit}, Temperature) = () \rightarrow \text{String}$
- ▶  $mtype(dHigh, Recording) = () \rightarrow \text{int}$
- ▶  $mtype(dHigh, Temperature) = () \rightarrow \text{int}$
- ▶  $override(dHigh, Object, ()) \rightarrow \text{int}$
- ▶  $override(dHigh, Recording, ()) \rightarrow \text{int}$
- ▶  $override(dHigh, Temperature, ()) \rightarrow \text{int}$
- ▶  $mbody(\text{unit}, Recording) = (\varepsilon, \text{"not set"})$
- ▶  $mtype(\text{unit}, Temperature) = (\varepsilon, \text{"°C"})$

# Operational Semantics

(definition of the evaluation steps)

# Direct Evaluation Steps

- Evaluation: relation  $t \longrightarrow t'$  for one evaluation step

$$\begin{array}{c}
 \text{E-PROJNEW} \\
 \frac{\text{fields}(C) = C_1 \ f_1, \dots}{(\mathbf{new} \ C(v_1, \dots)).f_i \longrightarrow v_i} \\
 \text{E-INVKNW} \\
 \frac{\text{mbody}(m, C) = (x_1 \ \dots, \ t)}{\longrightarrow t[\mathbf{new} \ C(v_1, \dots)/\mathbf{this}, u_1, \dots/x_1, \dots]}
 \end{array}$$

$$\begin{array}{c}
 \text{E-CASTNEW} \\
 \frac{C \leqslant D}{(D)(\mathbf{new} \ C(v_1, \dots)) \longrightarrow \mathbf{new} \ C(v_1, \dots)}
 \end{array}$$

# Evaluation Steps in Context

$$\frac{\text{E-FIELD} \quad t \longrightarrow t'}{t.f \longrightarrow t'.f}$$

$$\frac{\text{E-INVK-RECV} \quad t \longrightarrow t'}{t.m(t_1, \dots) \longrightarrow t'.m(t_1, \dots)}$$

$$\frac{\text{E-INVK-ARG} \quad t_i \longrightarrow t'_i}{v.m(v_1, \dots, t_i, \dots) \longrightarrow v.m(v_1, \dots, t'_i, \dots)}$$

$$\frac{\text{E-NEW-ARG} \quad t_i \longrightarrow t'_i}{\mathbf{new} \ C(v_1, \dots, t_i, \dots) \longrightarrow \mathbf{new} \ C(v_1, \dots, t'_i, \dots)}$$

$$\frac{\text{E-CAST} \quad t \longrightarrow t'}{(C)t \longrightarrow (C)t'}$$

## Example: Evaluation Steps

```
((Pair) (new Pair (new Pair (new A(), new B()).setfst (new B()), new B()).fst)).fst
```

```
// → [E-Field], [E-Cast], [E-New-Arg], [E-InvkNew]
```

```
((Pair) (new Pair (new Pair (new B(), new B()), new B()).fst)).fst
```

```
// → [E-Field], [E-Cast], [E-ProjNew]
```

```
((Pair) (new Pair (new B(), new B()))).fst
```

```
// → [E-Field], [E-CastNew]
```

```
(new Pair (new B(), new B()))).fst
```

```
// → [E-ProjNew]
```

```
new B()
```

# Typing Rules

# Typing Rules

## Overview of typing judgments

- ▶  $C <: D$   
 $C$  is subtype of  $D$
- ▶  $A \vdash t : C$   
 Under type assumption  $A$ , the expression  $t$  has type  $C$ .
- ▶  $F m(C_1 x_1, \dots) \{\mathbf{return} t; \}$  OK in  $C$   
 Method declaration is accepted in class  $C$ .
- ▶ **class**  $C$  **extends**  $D \{C_1 f_1; \dots K M_1 \dots \}$  OK  
 Class declaration is accepted
- ▶ Type assumptions defined by

$$A ::= \emptyset \mid A, x : C$$



## Accepted Class Declaration

$$\frac{
 \begin{array}{l}
 K = C(D_1 \ g_1, \dots, C_1 \ f_1, \dots) \{ \mathbf{super}(g_1, \dots); \mathbf{this}.f_1 = f_1; \dots \} \\
 \text{fields}(D) = D_1 \ g_1 \dots \quad (\forall j) \ M_j \text{ OK in } C
 \end{array}
 }{
 \mathbf{class } C \ \mathbf{extends } D \ \{ C_1 \ f_1; \dots \ K \ M_1 \dots \}
 }$$

## Accepted Method Declaration

$$\frac{x_1 : C_1, \dots, \text{this} : C \vdash t : E \quad E \triangleleft: F}{CT(C) = \mathbf{class} \ C \ \mathbf{extends} \ D \dots \quad \mathit{override}(m, D, (C_1, \dots)) \rightarrow F}$$

$$F \ m(C_1 \ x_1, \dots) \ \{\mathbf{return} \ t; \} \ \text{OK in } C$$

## Expression Has Type

$$\frac{\text{T-VAR} \quad x : C \in A}{A \vdash x : C}$$

$$\frac{\text{T-FIELD} \quad A \vdash t : C \quad \text{fields}(C) = C_1 f_1, \dots}{A \vdash t.f_j : C_j}$$

$$\frac{\text{F-INVK} \quad A \vdash t : C \quad (\forall i) A \vdash t_i : C_i \quad (\forall i) C_i \leq D_i \quad \text{mtype}(m, C) = (D_1, \dots) \rightarrow D}{A \vdash t.m(t_1, \dots) : D}$$

$$\frac{\text{F-NEW} \quad (\forall i) A \vdash t_i : C_i \quad (\forall i) C_i \leq D_i \quad \text{fields}(C) = D_1 f_1, \dots}{A \vdash \mathbf{new} C(t_1, \dots) : C}$$

# Type Rules for Type Casts

$$\frac{\text{T-UCAST} \quad A \vdash t : D \quad D \leqslant C}{A \vdash (C)t : C}$$

$$\frac{\text{T-DCAST} \quad A \vdash t : D \quad C \leqslant D \quad C \neq D}{A \vdash (C)t : C}$$

# Type Safety for Featherweight Java

- ▶ “Preservation” and “Progress” yields type safety
- ▶ “Preservation”:  
If  $A \vdash t : C$  and  $t \longrightarrow t'$ , then  $A \vdash t' : C'$  with  $C' \leq C$ .
- ▶ “Progress”: (short version)  
If  $A \vdash t : C$ , then  $t \longrightarrow t'$ , for some  $t'$ , or  $t \equiv v$  is a value, or  $t$  contains a subexpression  $e'$

$$e' \equiv (C)(\mathbf{new} \ D(v_1, \dots))$$

with  $D \not\leq C$ .

- ⇒
- ▶ All method calls and field accesses evaluate without errors.
  - ▶ Type casts can fail.

# Problems in the Preservation Proof

## Type casts destroy preservation

- ▶ Consider the expression  $(A) ((\text{Object})\text{new } B())$
- ▶ It holds that  $\emptyset \vdash (A) ((\text{Object})\text{new } B()): A$
- ▶ It holds that  $(A) ((\text{Object})\text{new } B()) \longrightarrow (A) (\text{new } B())$
- ▶ But  $(A) (\text{new } B())$  has no type!

# Problems in the Preservation Proof

## Type casts destroy preservation

- ▶ Consider the expression  $(A) ((\text{Object})\text{new } B())$
- ▶ It holds that  $\emptyset \vdash (A) ((\text{Object})\text{new } B()): A$
- ▶ It holds that  $(A) ((\text{Object})\text{new } B()) \longrightarrow (A) (\text{new } B())$
- ▶ But  $(A) (\text{new } B())$  has no type!
- ▶ Workaround: add additional rule for this case “*stupid cast*”  
—subsequent evaluation step fails

$$\frac{\text{T-SCAST} \quad A \vdash t : D \quad C \not\vdash D \quad D \not\vdash C}{A \vdash (C)t : C}$$

- ▶ We can prove preservation with this rule.

## Statement of Type Safety

If  $A \vdash t : C$ , then one of the following cases applies:

1.  $t$  does not terminate  
i.e., there exists an infinite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow t_2 \longrightarrow \dots$$

2.  $t$  evaluates to a value  $v$  after a finite number of evaluation steps  
i.e., there exists a finite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow \dots \longrightarrow t_n = v$$

3.  $t$  gets stuck at a failing cast  
i.e., there exists a finite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow \dots \longrightarrow t_n$$

where  $t_n$  contains a subterm  $(C)(\mathbf{new} D(v_1, \dots))$  such that  $D \not\prec C$ .